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## **ON HARARY ENERGY OF GRAPHS**

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**Abstract:** The Harary matrix of a connected graph G is defined as  $H(G) = [a_{ij}]_{n \times n}$ , where  $a_{ij} = \frac{1}{d(v_i, v_j)}$ ; for  $v_i$  and  $v_j$  are non adjacent in G and  $a_{ii} = 0$ ; for all  $i, j = 1, 2, 3, \dots, n$ . The Harary energy of G is the sum of the absolute values of the eigenvalues of Harary matrix of G. In this paper, the Harary characteristic polynomial of  $K_{m,n}$  and Harary energy of some graphs are investigated.

Keywords and Phrases: Eigenvalue, Graph Polynomial, Graph Energy.

2020 Mathematics Subject Classification: 05C50, 05C31, 05C76.

## 1. Introduction and Preliminaries

Let G be a simple, undirected and connected graph with vertex set  $V(G) = \{v_1, v_2, v_3, \dots, v_n\}$ . The distance between two vertices  $v_i$  and  $v_j$  is the length of shortest path between them; for all  $1 \leq i, j \leq j$ . The maximum distance between any pair of vertices is known as diameter of graph G. For standard terminology and notations in graph theory, rely upon West [14] while for any undefined term related to energy of graphs, refer to Gutman [6].

**Definition 1.1.** The m-Shadow graph,  $D_m(G)$  of a connected graph G is constructed by taking m copies of G say  $G_1, G_2, ..., G_m$ . Then Join each vertex u in