# ON HARARY ENERGY OF GRAPHS 

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Abstract: The Harary matrix of a connected graph $G$ is defined as $H(G)=$ $\left[a_{i j}\right]_{n \times n}$, where $a_{i j}=\frac{1}{d\left(v_{i}, v_{j}\right)}$; for $v_{i}$ and $v_{j}$ are non adjacent in $G$ and $a_{i i}=0$; for all $i, j=1,2,3, \cdots, n$. The Harary energy of $G$ is the sum of the absolute values of the eigenvalues of Harary matrix of $G$. In this paper, the Harary characteristic polynomial of $K_{m, n}$ and Harary energy of some graphs are investigated.
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## 1. Introduction and Preliminaries

Let $G$ be a simple, undirected and connected graph with vertex set $V(G)=$ $\left\{v_{1}, v_{2}, v_{3}, \cdots, v_{n}\right\}$. The distance between two vertices $v_{i}$ and $v_{j}$ is the length of shortest path between them; for all $1 \leq i, j \leq j$. The maximum distance between any pair of vertices is known as diameter of graph $G$. For standard terminology and notations in graph theory, rely upon West [14] while for any undefined term related to energy of graphs, refer to Gutman [6].
Definition 1.1. The $m$-Shadow graph, $D_{m}(G)$ of a connected graph $G$ is constructed by taking $m$ copies of $G$ say $G_{1}, G_{2}, \ldots, G_{m}$. Then Join each vertex u in

